

# Scalable Relational Learning for Large Heterogeneous Networks

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## Abstract

Relational models for heterogeneous network data are becoming increasingly important for many real-world applications. However, existing relational learning approaches are not parallel, have scalability issues, and thus unable to handle large heterogeneous network data. In this paper, we propose parallel Collective Matrix Factorization (PCMF) that serves as a fast and flexible framework for joint modeling of large heterogeneous networks. The PCMF learning algorithm solves for a single parameter given the others, leading to a *parallel scheme* that is fast, flexible, and general for a variety of relational learning tasks and heterogeneous data types. The proposed approach is carefully designed to be (a) efficient for large heterogeneous networks (linear in the total number of observations from the set of input matrices), (b) flexible as many components are interchangeable and easily adaptable, and (c) effective for a variety of applications as well as for different types of data. The experiments demonstrate the scalability, flexibility, and effectiveness of PCMF. For instance, we show that PCMF outperforms a recent state-of-the-art parallel approach in runtime, scalability, and prediction quality. Finally, the effectiveness of PCMF is shown on a number of relational learning tasks such as serving predictions in a real-time streaming fashion.

TABLE I. DATASET STATISTICS

graph datasets	(semantics) node & edge types	$m$	$n$	$ \Omega $	max		$\bar{d}_{out}$	$\bar{d}_{in}$	weight			$\rho$	$ \Omega^{test} $
					$d_{out}$	$d_{in}$			range	$\mu_{out}$	$\mu_{in}$		
amazon	users-rate-items	2.1M	1.2M	4.7M	9.8k	2.5k	2.18	3.79	1-5	3.57	3.77	$10^{-6}$	1.2M
dating	users-rate-users	135k	169k	16M	24k	32k	121.83	97.7	1-10	5.93	6.03	<0.01	868k
eachmovie	users-rate-movies	1.6k	74k	2.2M	26k	1.2k	1.4k	30.22	1-6	3.99	3.45	0.02	562k
epinions	users-rate-items	120k	756k	13M	159k	1.2k	111.18	17.73	1-5	4.64	4.31	<0.01	137k
	users-trust-users	120k	120k	607k	1.8k	3.2k	5.03	5.03	1	0.47	0.35	$10^{-5}$	
flickr	users-friend-users	1.9M	1.9M	18M	21k	13k	9.72	9.72	1	0.68	0.8	$10^{-6}$	
	users-join-group	1.7M	104k	8.5M	2.2k	35k	4.94	82.45	1	0.23	1	$10^{-5}$	4.5M
lastfm	users-listento-songs	992	1.1M	15M	146k	14k	15k	14.13	1	1	0.93	0.01	
	users-listento-band	992	174k	19M	183k	115k	19k	110.01	1	1	1	0.11	3.8M
livejournal	users-friend-users	5.2M	5.2M	39M	12k	928	7.56	7.56	1	0.55	0.95	$10^{-6}$	
	users-join-groups	3.2M	7.5M	112M	300	1.1M	35.08	15	1	1	1	$10^{-6}$	9.8M
movielens10M	users-rate-movies	72k	65k	9.3M	7.3k	29k	129.97	142.8	0.5-5	3.42	0.52	<0.01	699k
stackoverflow	users-favorite-posts	545k	97k	1.0M	4.0k	4.9k	1.91	10.78	1	0.86	0.92	$10^{-5}$	260k
yelp	users-rate-businesses	230k	12k	225k	575	824	0.98	19.53	1-5	0.73	3.66	$10^{-5}$	4.6k
youtube	users-friend-users	1.2M	1.2M	4.0M	23k	20k	3.42	3.42	1	0.46	0.86	$10^{-6}$	
	users-join-groups	664k	30k	293k	1.0k	7.6k	0.44	9.75	1	0.14	1	$10^{-5}$	989k